場合の数(グループ分け)について

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Example 7 人の生徒 a,b,c,d,e,f,g を次のように分ける.

3人, 2人, 2人の3つの組に分ける.

$ \boxed{ a,b,c } \boxed{ d,e } \boxed{ f,g } $		$\boxed{\text{a,b,c}} \boxed{\text{d,g}} \boxed{\text{e,f}}$
[a,b,d] $[c,e]$ $[f,g]$	a,b,d c,f e,g	a,b,d c,g e,f
[a,b,e] $[c,d]$ $[f,g]$	$\boxed{\text{a,b,e}} \boxed{\text{c,f}} \boxed{\text{d,g}}$	$egin{bmatrix} a,b,e \ \hline \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
[a,b,f] $[c,d]$ $[e,g]$	a,b,f c,e d,g	a,b,f c,g d,e
[a,b,g] $[c,d]$ $[e,f]$	a,b,g c,e d,f	a,b,g c,f d,e
[a,c,d] $[b,e]$ $[f,g]$		$oxed{a,c,d}$ $oxed{b,g}$ $oxed{e,f}$
[a,c,e] $[b,d]$ $[f,g]$	a,c,e b,f d,g	[a,c,e] $[b,g]$ $[d,f]$
[a,c,f] $[b,d]$ $[e,g]$	$egin{bmatrix} a,c,f \end{bmatrix}$ $egin{bmatrix} b,e \end{bmatrix}$ $egin{bmatrix} d,g \end{bmatrix}$	$ \boxed{\text{a,c,f}} \ \boxed{\text{b,g}} \ \boxed{\text{d,e}} $
[a,c,g] [b,d] [f,g]	a,c,g b,f d,g	a,c,g b,g d,f
[a,d,e] $[b,c]$ $[f,g]$	[a,d,e] [b,f] [c,g]	[a,d,e] $[b,g]$ $[c,f]$
[a,d,f] $[b,c]$ $[e,g]$		$oxed{a,d,f} oxed{b,g} oxed{c,e}$
[a,d,g] $[a,c]$ $[e,f]$	a,d,g b,e c,f	[a,d,g] $[b,f]$ $[c,e]$
a,e,f b,c d,g	a,e,f b,d e,g	[a,e,f] $[b,g] $ $[c,d]$
[a,e,g] $[b,c]$ $[d,f]$	[a,e,g] [b,d] [c,f]	[a,e,g] [b,f] [c,d]
[a,f,g] $[b,c]$ $[d,e]$	a,f,g b,d c,e	a,f,g b,e c,e

b,c,d a,e f,g	[b,c,d] $[a,f]$ $[e,g]$	$oxed{b,c,d}$ $oxed{a,g}$ $oxed{e,f}$
[b,c,e] $[a,d]$ $[f,g]$	[b,c,e] $[a,f]$ $[d,g]$	$oxed{b,c,e}$ $oxed{a,g}$ $oxed{d,f}$
[b,c,f] $[a,d]$ $[e,g]$	[b,c,f] $[a,e]$ $[d,g]$	[b,c,f] $[a,g]$ $[d,e]$
b,c,g a,d e,f	[b,c,g] $[a,e]$ $[d,f]$	$oxed{b,c,g}$ $oxed{a,f}$ $oxed{d,e}$
b,d,e a,c f,g	[b,d,e] $[a,f]$ $[c,g]$	[b,d,e] $[a,g]$ $[c,f]$
[b,d,f] $[a,c]$ $[e,g]$	[b,d,f] $[a,e]$ $[c,g]$	[b,d,f] $[a,g]$ $[c,e]$
[b,d,g] $[a,c]$ $[e,f]$	[b,d,g] $[a,e]$ $[c,f]$	[b,d,g] $[a,f]$ $[c,e]$
[b,e,f] $[a,c]$ $[d,g]$	b,e,f a,d c,g	b,e,f a,g c,d
[b,e,g] $[a,c]$ $[d,f]$	[b,e,g] [a,d] [c,f]	$egin{bmatrix} \mathbf{b},\mathbf{e},\mathbf{g} \end{bmatrix}$ $egin{bmatrix} \mathbf{a},\mathbf{f} \end{bmatrix}$ $egin{c} \mathbf{c},\mathbf{d} \end{bmatrix}$
[b,f,g] $[a,c]$ $[d,e]$	[b,f,g] $[a,d]$ $[c,e]$	b,f,g a,e c,d
c,d,e a,b f,g		
c,d,f a,b e,g	[c,d,f] $[a,e]$ $[b,g]$	c,d,f a,g b,e
[c,d,g] $[a,b]$ $[e,f]$	[c,d,g] $[a,e]$ $[b,f]$	
c,e,f a,b d,g	$ \begin{bmatrix} c,e,f \end{bmatrix} $ $ \begin{bmatrix} a,d \end{bmatrix} $ $ \begin{bmatrix} b,g \end{bmatrix} $	$ \begin{bmatrix} c,e,f \end{bmatrix} $ $ \begin{bmatrix} a,g \end{bmatrix} $ $ \begin{bmatrix} b,d \end{bmatrix} $
[c,e,g] $[a,b] $ $[d,f]$		
$ \boxed{ \mathrm{c,f,g} } $	$ \boxed{ \text{c,f,g} } \boxed{ \text{a,d} } \boxed{ \text{b,e} } $	c,f,g a,e b,d
$\boxed{\mathrm{d,e,f}}$ $\boxed{\mathrm{a,b}}$ $\boxed{\mathrm{c,g}}$	$\boxed{\text{d,e,f}} \boxed{\text{a,c}} \boxed{\text{b,g}}$	$\boxed{\mathrm{d,e,f}}$ $\boxed{\mathrm{a,g}}$ $\boxed{\mathrm{b,c}}$
$\boxed{\text{d,e,g}} \boxed{\text{a,b}} \boxed{\text{c,f}}$	[d,e,g] $[a,c]$ $[b,f]$	$\boxed{\text{d,e,g}} \boxed{\text{a,f}} \boxed{\text{b,c}}$
$\boxed{\mathrm{d,f,g}} \boxed{\mathrm{a,b}} \boxed{\mathrm{c,e}}$	$oxed{d,f,g}$ $oxed{a,c}$ $oxed{b,e}$	$\boxed{\mathrm{d,f,g}}$ $\boxed{\mathrm{a,e}}$ $\boxed{\mathrm{b,c}}$
$egin{bmatrix} { m e,f,g} \ \hline \ { m a,b} \ \hline \ { m c,d} \ \hline \ \end{array}$	e,f,g a,c b,d	$egin{bmatrix} e,f,g & a,d & b,c \end{bmatrix}$

$$\frac{{}_{7}{\rm C}_{3} \cdot {}_{4}{\rm C}_{2} \cdot {}_{2}{\rm C}_{2}}{2!} = 105 \; (通り)$$